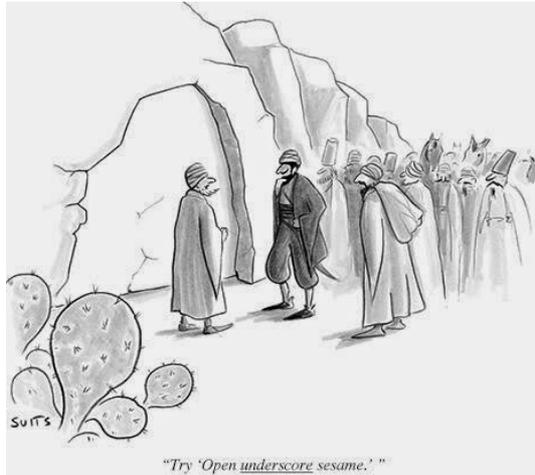


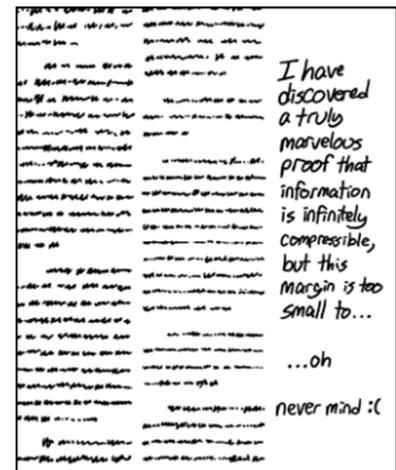
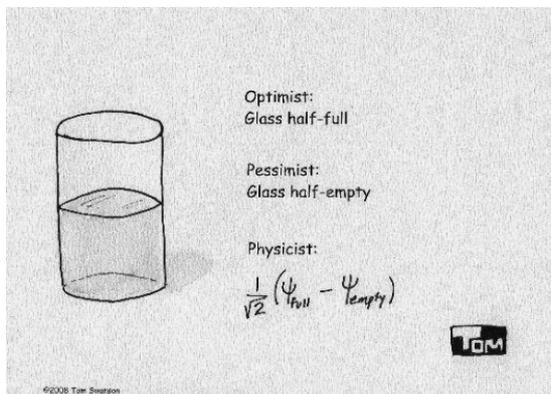
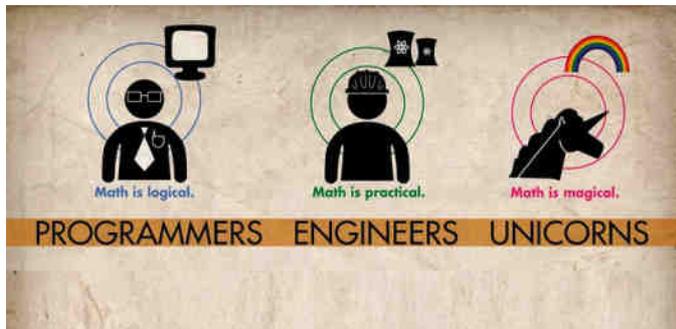
$$x^4 - 8228x^3 + 25385534x^2 - 34806653332x + 17895175197705 = 0$$



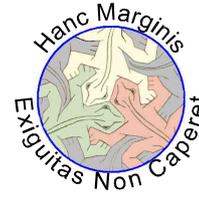
"Try 'Open underscore sesame.' "

## 10 Facts about you

1. You're reading this right now.
2. You're realizing that is a stupid fact.
4. You didn't notice I skipped three.
5. You're checking now.
6. You're smiling.
7. You're still reading this even though its stupid.
9. You didn't realize I skipped eight.
10. You're checking again and smiling about how you fell for it again.
11. You're enjoying this.
12. You didn't realize there's only supposed to be ten facts.



|                                      |    |                                              |                                                  |                                        |  |
|--------------------------------------|----|----------------------------------------------|--------------------------------------------------|----------------------------------------|--|
| 1                                    | T  | (1803) Guglielmo Libri Carucci dalla Sommaja | RM132                                            |                                        |  |
|                                      |    | (1878) Agner Krarup Erlang                   |                                                  |                                        |  |
|                                      |    | (1894) Satyendranath Bose                    | RM168                                            |                                        |  |
|                                      |    | (1912) Boris Gnedenko                        |                                                  |                                        |  |
| 2                                    | F  | (1822) Rudolf Julius Emmanuel Clausius       |                                                  |                                        |  |
|                                      |    | (1905) Lev Genrichovich Shnirelman           |                                                  |                                        |  |
|                                      |    | (1938) Anatoly Samoilenko                    |                                                  |                                        |  |
| 3                                    | S  | (1917) Yuri Alexeievich Mitropolsky          |                                                  |                                        |  |
| 4                                    | S  | (1643) Isaac Newton                          | RM071                                            |                                        |  |
| 2                                    | 5  | M                                            | (1723) Nicole-Reine Etable de Labrière Lepaute   |                                        |  |
|                                      |    |                                              | (1838) Marie Ennemond Camille Jordan             |                                        |  |
|                                      |    |                                              | (1871) Federigo Enriques                         | RM084                                  |  |
|                                      |    |                                              | (1871) Gino Fano                                 |                                        |  |
|                                      |    |                                              | (1871) Gino Fano                                 |                                        |  |
|                                      | 6  | T                                            | (1807) Jozeph Mitza Petzval                      |                                        |  |
|                                      |    |                                              | (1841) Rudolf Sturm                              |                                        |  |
|                                      | 7  | W                                            | (1871) Felix Edouard Justin Emile Borel          |                                        |  |
|                                      |    |                                              | (1907) Raymond Edward Alan Christopher Paley     |                                        |  |
|                                      | 8  | T                                            | (1888) Richard Courant                           | RM156                                  |  |
|                                      |    |                                              | (1924) Paul Moritz Cohn                          |                                        |  |
| (1942) Stephen William Hawking       |    |                                              |                                                  |                                        |  |
| 9                                    | F  | (1864) Vladimir Adreievich Steklov           |                                                  |                                        |  |
|                                      |    | (1915) Mollie Orshansky                      |                                                  |                                        |  |
| 10                                   | S  | (1875) Issai Schur                           |                                                  |                                        |  |
|                                      |    | (1905) Ruth Moufang                          |                                                  |                                        |  |
| 11                                   | S  | (1545) Guidobaldo del Monte                  | RM120                                            |                                        |  |
|                                      |    | (1707) Vincenzo Riccati                      |                                                  |                                        |  |
|                                      |    | (1734) Achille Pierre Dionis du Sejour       |                                                  |                                        |  |
| 3                                    | 12 | M                                            | (1906) Kurt August Hirsch                        |                                        |  |
|                                      |    |                                              | (1915) Herbert Ellis Robbins                     | RM156                                  |  |
|                                      | 13 | T                                            | (1864) Wilhelm Karl Werner Otto Fritz Franz Wien |                                        |  |
|                                      |    |                                              | (1876) Luther Pfahler Eisenhart                  |                                        |  |
|                                      |    |                                              | (1876) Erhard Schmidt                            |                                        |  |
|                                      |    |                                              | (1902) Karl Menger                               |                                        |  |
|                                      | 14 | W                                            | (1902) Alfred Tarski                             | RM096                                  |  |
|                                      | 15 | T                                            | (1704) Johann Castillon                          |                                        |  |
|                                      |    |                                              | (1717) Mattew Stewart                            |                                        |  |
|                                      |    |                                              | (1850) Sofia Vasilievna Kovalevskaja             | RM144                                  |  |
|                                      | 16 | F                                            | (1801) Thomas Klausen                            |                                        |  |
|                                      |    |                                              | (1647) Catherina Elisabetha Koopman Hevelius     |                                        |  |
|                                      | 17 | S                                            | (1847) Nikolay Egorovich Zukowsky                |                                        |  |
|                                      |    |                                              | (1858) Gabriel Koenigs                           |                                        |  |
|                                      | 18 | S                                            | (1856) Luigi Bianchi                             |                                        |  |
|                                      |    |                                              | (1880) Paul Ehrenfest                            |                                        |  |
|                                      | 4  | 19                                           | M                                                | (1813) Rudolf Friedrich Alfred Clebsch |  |
|                                      |    |                                              |                                                  | (1879) Guido Fubini                    |  |
| (1908) Aleksandr Gennadievich Kurosh |    |                                              |                                                  |                                        |  |
| 20                                   |    | T                                            | (1775) André Marie Ampère                        |                                        |  |
|                                      |    |                                              | (1895) Gabor Szegő                               |                                        |  |
|                                      |    |                                              | (1904) Renato Caccioppoli                        | RM072                                  |  |
| 21                                   |    | W                                            | (1846) Pieter Hendrik Schoute                    |                                        |  |
|                                      |    |                                              | (1915) Yuri Vladimirovich Linnik                 |                                        |  |
| 22                                   |    | T                                            | (1592) Pierre Gassendi                           |                                        |  |
|                                      |    |                                              | (1886) John William Navin Sullivan               |                                        |  |
|                                      |    |                                              | (1908) Lev Davidovich Landau                     | RM063                                  |  |
| 23                                   |    | F                                            | (1840) Ernst Abbe                                |                                        |  |
|                                      |    |                                              | (1862) David Hilbert                             | RM060                                  |  |
| 24                                   |    | S                                            | (1891) Abram Samoilovitch Besicovitch            |                                        |  |
|                                      |    |                                              | (1914) Vladimir Petrovich Potapov                |                                        |  |
| 25                                   | S  | (1627) Robert Boyle                          |                                                  |                                        |  |
|                                      |    | (1736) Joseph-Louis Lagrange                 | RM048                                            |                                        |  |
|                                      |    | (1843) Karl Hermann Amandus Schwarz          |                                                  |                                        |  |
| 5                                    | 26 | M                                            | (1799) Benoît Paul Émile Clapeyron               |                                        |  |
|                                      |    |                                              | (1862) Eliakim Hastings Moore                    |                                        |  |
|                                      | 27 | T                                            | (1832) Charles Lutwidge Dodgson                  | RM108                                  |  |
|                                      | 28 | W                                            | (1701) Charles Marie de La Condamine             |                                        |  |
|                                      |    |                                              | (1888) Louis Joel Mordell                        |                                        |  |
|                                      |    |                                              | (1892) Carlo Emilio Bonferroni                   |                                        |  |
|                                      | 29 | T                                            | (1817) William Ferrel                            |                                        |  |
|                                      |    |                                              | (1888) Sidney Chapman                            |                                        |  |
|                                      | 30 | F                                            | (1619) Michelangelo Ricci                        |                                        |  |
|                                      | 31 | S                                            | (1715) Giovanni Francesco Fagnano dei Toschi     |                                        |  |
| (1841) Samuel Loyd                   |    |                                              |                                                  |                                        |  |
| (1896) Sofia Alexandrovna Janovskaja |    |                                              |                                                  |                                        |  |
| (1945) Persi Warren Diaconis         |    |                                              | RM180                                            |                                        |  |
| (1900) John Charles Burkill          |    |                                              |                                                  |                                        |  |
| (1522) Lodovico Ferrari              |    |                                              |                                                  |                                        |  |



**Putnam 2000, A1**

Let  $A$  be a positive real number. What are the possible values of  $\sum_{i=0}^{\infty} x_i^2$ , given that  $x_0, x_1, \dots$  are positive

numbers for which  $\sum_{i=0}^{\infty} x_i = A$ ?

**English Jokes that only intellectuals understand**

It's hard to explain puns to kleptomaniacs because they always take things, *literally*.

**Headlines from a Mathematical World**

*After Switch in Standardized Tests, Scores Drop.*

Mathematical World: After Switch in Standardized Tests, Scores No Longer Directly Comparable.

*Alice laughed: "There's no use trying," she said; "one can't believe impossible things."*

*"I daresay you haven't had much practice," said the Queen. "When I was younger, I always did it for half an hour a day. Why, sometimes I've believed as many as six impossible things before breakfast."*

Charles Lutwidge Dodgson

*If you want to inspire confidence, give plenty of statistics. It does not matter that they should be accurate, or even intelligible, as long as there is enough of them.*

Charles Lutwidge Dodgson

*A formal manipulator in mathematics often experiences the discomforting feeling that his pencil surpasses him in intelligence.*

Howard W. Eves

*One can measure the importance of a scientific work by the number of earlier publications rendered superfluous by it.*

David Hilbert

*Depriving a mathematical of the chance to making demonstrations ad absurdum would be equal to tie the hands of a boxer behind his back.*

David Hilbert

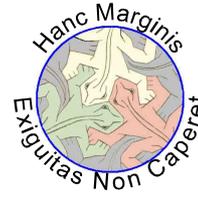
*Actually mathematics require much imagination: it is impossible to be a mathematician without being a poet in soul.*

Sofia Vasilievna Kovalevskaja

*[said about the chemist Lavoisier:] It took the mob only a moment to remove his head; a century will not suffice to reproduce it.*

Joseph-Louis Lagrange

|    |    |                                                                                                                                           |                                                                                                      |
|----|----|-------------------------------------------------------------------------------------------------------------------------------------------|------------------------------------------------------------------------------------------------------|
| 1  | S  | (1900) John Charles Burkill                                                                                                               |                                                                                                      |
| 6  | 2  | M                                                                                                                                         | (1522) Lodovico Ferrari<br>(1893) Cornelius Lanczos<br>(1897) Gertrude Blanch                        |
| 3  | T  | (1893) Gaston Maurice Julia                                                                                                               | RM073                                                                                                |
| 4  | W  | (1905) Eric Christopher Zeeman                                                                                                            |                                                                                                      |
| 5  | T  | (1757) Jean Marie Constant Duhamel                                                                                                        |                                                                                                      |
| 6  | F  | (1465) Scipione del Ferro<br>(1612) Antoine Arnauld<br>(1695) Nicolaus (II) Bernoulli                                                     | RM064<br>RM093                                                                                       |
| 7  | S  | (1877) Godfried Harold Hardy<br>(1883) Eric Temple Bell                                                                                   | RM049                                                                                                |
| 8  | S  | (1700) Daniel Bernoulli<br>(1875) Francis Ysidro Edgeworth<br>(1928) Ennio de Giorgi                                                      | RM093<br>RM133                                                                                       |
| 7  | 9  | M                                                                                                                                         | (1775) Farkas Wolfgang Bolyai<br>(1907) Harold Scott Macdonald Coxeter                               |
| 10 | T  | (1747) Aida Yasuaki<br>(1932) Vivienne Malone-Mayes                                                                                       | RM097<br>RM121                                                                                       |
| 11 | W  | (1657) Bernard Le Bovier de Fontenelle<br>(1800) William Henry Fox Talbot<br>(1839) Josiah Willard Gibbs<br>(1915) Richard Wesley Hamming |                                                                                                      |
| 12 | T  | (1914) Hanna Caemmerer Neumann<br>(1921) Kathleen Rita McNulty Mauchly Antonelli                                                          |                                                                                                      |
| 13 | F  | (1805) Johann Peter Gustav Lejeune Dirichlet                                                                                              | RM145                                                                                                |
| 14 | S  | (1468) Johann Werner<br>(1849) Hermann Hankel<br>(1877) Edmund Georg Hermann Landau<br>(1896) Edward Artur Milne                          | RM063                                                                                                |
| 15 | S  | (1564) Galileo Galilei<br>(1850) Sophie Willock Bryant<br>(1861) Alfred North Whitehead<br>(1946) Douglas Hofstadter                      | RM085                                                                                                |
| 8  | 16 | M                                                                                                                                         | (1822) Francis Galton<br>(1853) Gregorio Ricci-Curbastro<br>(1903) Beniamino Segre                   |
| 17 | T  | (1890) Sir Ronald Aylmer Fisher<br>(1891) Adolf Abraham Halevi Fraenkel<br>(1905) Rózsa Péter                                             |                                                                                                      |
| 18 | W  | (1404) Leon Battista Alberti<br>(1919) Clifford Truesdell                                                                                 | RM157                                                                                                |
| 19 | T  | (1473) Nicolaus Copernicus                                                                                                                | RM181                                                                                                |
| 20 | F  | (1844) Ludwig Boltzmann                                                                                                                   | RM061                                                                                                |
| 21 | S  | (1591) Girard Desargues<br>(1915) Evgeny Michailovich Lifshitz                                                                            |                                                                                                      |
| 22 | S  | (1857) Heinrich Rudolf Hertz<br>(1903) Frank Plumpton Ramsey                                                                              |                                                                                                      |
| 9  | 23 | M                                                                                                                                         | (1583) Jean-Baptiste Morin<br>(1922) Anneli Cahn Lax<br>(1951) Shigefumi Mori<br>(1561) Henry Briggs |
| 24 | T  | (1871) Felix Bernstein                                                                                                                    | RM169                                                                                                |
| 25 | W  | (1827) Henry Watson                                                                                                                       |                                                                                                      |
| 26 | T  | (1786) Dominique Francois Jean Arago                                                                                                      |                                                                                                      |
| 27 | F  | (1881) Luitzen Egbertus Jan Brouwer                                                                                                       |                                                                                                      |
| 28 | S  | (1735) Alexandre Theophile Vandermonde                                                                                                    |                                                                                                      |
| 29 |    | (1860) Herman Hollerith                                                                                                                   | RM109                                                                                                |



**Putnam 2000, A2**

Prove that there exist infinitely many integers  $n$  such that  $n$ ,  $n + 1$ ,  $n + 2$  are each the sum of the squares of two integers.

**English Jokes that only intellectuals understand**

Three logicians walk into a bar. The bartender ask: "Do all of you want a drink?"

The first logician says: "I don't know"

The second logician says: "I don't know"

The third logician says: "Yes!"

**Headlines from a Mathematical World**

*Controversial Program Would Cost \$50 Million in Taxpayer Money.*

Mathematical World: Controversial Program Would Cost 0.0001% of Taxpayer Money.

*The Handmaiden of the Sciences. [Book by that title.]*  
Eric Temple Bell

*The cowboys have a way of trussing up a steer or a pugnacious bronco which fixes the brute so that it can neither move nor think. This is the hog-tie, and it is what Euclid did to geometry.*

Eric Temple Bell

*Hofstadter's Law: It always takes longer than you expect, even when you take into account Hofstadter's Law.*

Douglas Hofstadter

*[Asked for a testimony to the effect that Emmy Noether was a great woman mathematician, he said:]*

*I can testify that she is a great mathematician, but that she is a woman, I cannot swear.*

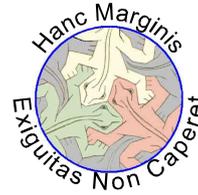
Edmund Georg Hermann Landau

*This article gives wrong solutions to trivial problems. The main mistake, however, is not new.*

Clifford Truesdell

*Mathematics as a science, commenced when first someone, probably a Greek, proved propositions about "any" things or about "some" things, without specifications of definite particular things.*

Alfred North Whitehead



|    |    |                                                                                                                                                         |                                                                                                             |                                                                                           |                                                                                          |
|----|----|---------------------------------------------------------------------------------------------------------------------------------------------------------|-------------------------------------------------------------------------------------------------------------|-------------------------------------------------------------------------------------------|------------------------------------------------------------------------------------------|
| 1  | S  | (1611) John Pell<br>(1879) Robert Daniel Carmichael                                                                                                     |                                                                                                             |                                                                                           |                                                                                          |
| 10 | 2  | M                                                                                                                                                       | (1836) Julius Weingarten                                                                                    |                                                                                           |                                                                                          |
|    | 3  | T                                                                                                                                                       | (1838) George William Hill<br>(1845) Georg Cantor<br>(1916) Paul Richard Halmos                             |                                                                                           |                                                                                          |
|    |    |                                                                                                                                                         | RM062                                                                                                       |                                                                                           |                                                                                          |
| 4  | W  | (1822) Jules Antoine Lissajous                                                                                                                          |                                                                                                             |                                                                                           |                                                                                          |
| 5  | T  | (1512) Gerardus Mercator<br>(1759) Benjamin Gompertz<br>(1817) Angelo Genocchi<br>(1885) Pauline Sperry<br>(1915) Laurent Schwartz<br>(1931) Vera Pless |                                                                                                             |                                                                                           |                                                                                          |
|    | 6  | F                                                                                                                                                       | (1866) Ettore Bortolotti                                                                                    |                                                                                           |                                                                                          |
|    | 7  | S                                                                                                                                                       | (1792) William Herschel<br>(1824) Delfino Codazzi<br>(1922) Olga Alexandrovna Ladyzhenskaya                 | RM146                                                                                     |                                                                                          |
|    |    | 8                                                                                                                                                       | S                                                                                                           | (1851) George Chrystal                                                                    |                                                                                          |
| 11 | 9  | M                                                                                                                                                       | (1818) Ferdinand Joachimsthal<br>(1900) Howard Hathaway Aiken                                               |                                                                                           |                                                                                          |
|    | 10 | T                                                                                                                                                       | (1864) William Fogg Osgood<br>(1872) Mary Ann Elizabeth Stephansen                                          |                                                                                           |                                                                                          |
| 11 | W  | (1811) Urbain Jean Joseph Le Verrier<br>(1853) Salvatore Pincherle<br>(1870) Louis Bachelier                                                            | RM158                                                                                                       |                                                                                           |                                                                                          |
|    | 12 | T                                                                                                                                                       | (1685) George Berkeley<br>(1824) Gustav Robert Kirchhoff<br>(1859) Ernesto Cesaro                           |                                                                                           |                                                                                          |
| 13 | F  | (1861) Jules Joseph Drach<br>(1957) Rudy D'Alembert                                                                                                     |                                                                                                             |                                                                                           |                                                                                          |
|    | 14 | S                                                                                                                                                       | (1864) Jozef Kurschak<br>(1879) Albert Einstein<br>(1904) Lyudmila Vsevolodovna Keldysh                     | RM074                                                                                     |                                                                                          |
| 15 |    | S                                                                                                                                                       | (1860) Walter Frank Raphael Weldon<br>(1868) Grace Chisolm Young                                            |                                                                                           |                                                                                          |
|    |    | 12                                                                                                                                                      | 16                                                                                                          | M                                                                                         | (1750) Caroline Herschel<br>(1789) Georg Simon Ohm<br>(1846) Magnus Gosta Mittag-Leffler |
| 17 | T  |                                                                                                                                                         | (1876) Ernest Benjamin Esclangon<br>(1897) Charles Fox                                                      |                                                                                           |                                                                                          |
| 18 | W  |                                                                                                                                                         | (1640) Philippe de La Hire<br>(1690) Christian Goldbach<br>(1796) Jacob Steiner<br>(1870) Agnes Sime Baxter | RM122                                                                                     |                                                                                          |
|    | 19 | T                                                                                                                                                       | (1862) Adolf Kneser<br>(1910) Jacob Wolfowitz                                                               |                                                                                           |                                                                                          |
| 20 | F  | (1840) Franz Mertens<br>(1884) Philip Franck<br>(1938) Sergi Petrovich Novikov                                                                          |                                                                                                             |                                                                                           |                                                                                          |
|    | 21 | S                                                                                                                                                       | (1768) Jean Baptiste Joseph Fourier<br>(1884) George David Birkhoff                                         |                                                                                           |                                                                                          |
| 22 |    | S                                                                                                                                                       | (1891) Lorna Mary Swain<br>(1917) Irving Kaplansky<br>(1944) Margaret Hilary Ashworth Millington            |                                                                                           |                                                                                          |
|    | 13 | 23                                                                                                                                                      | M                                                                                                           | (1754) Georg Freiherr von Vega<br>(1882) Emmy Amalie Noether<br>(1897) John Lighton Synge | RM050                                                                                    |
|    |    | 24                                                                                                                                                      | T                                                                                                           | (1809) Joseph Liouville<br>(1948) Sun-Yung (Alice) Chang<br>(1966) Gigliola Staffilani    | RM142                                                                                    |
| 25 |    |                                                                                                                                                         | W                                                                                                           | (1538) Christopher Clausius                                                               |                                                                                          |
| 26 | T  | (1848) Konstantin Andreev<br>(1913) Paul Erdős                                                                                                          | RM110                                                                                                       |                                                                                           |                                                                                          |
|    | 27 | F                                                                                                                                                       | (1857) Karl Pearson                                                                                         |                                                                                           |                                                                                          |
| 28 | S  | (1749) Pierre-Simon de Laplace<br>(1928) Alexander Grothendieck                                                                                         | RM086                                                                                                       |                                                                                           |                                                                                          |
|    | 29 | S                                                                                                                                                       | (1825) Francesco Faà Di Bruno<br>(1873) Tullio Levi-Civita<br>(1896) Wilhelm Ackerman                       | RM170<br>RM098                                                                            |                                                                                          |
| 14 |    | 30                                                                                                                                                      | M                                                                                                           | (1892) Stefan Banach<br>(1921) Alfréd Rényi                                               | RM134                                                                                    |
|    |    | 31                                                                                                                                                      | T                                                                                                           | (1596) René Descartes                                                                     |                                                                                          |

### Putnam 2000, A3

The octagon  $P_1 P_2 P_3 P_4 P_5 P_6 P_7 P_8$  is inscribed in a circle, with the vertices around the circumference in the given order. Given that the polygon  $P_1 P_3 P_5 P_7$  is a square of area 5, and the polygon  $P_2 P_4 P_6 P_8$  is a rectangle of area 4, find the maximum possible area of the octagon.

### English Jokes that only intellectuals understand

Einstein, Newton and Pascal are playing hide and seek. It's Einstein turn to count so he covers his eyes and start counting. Pascal runs off and hides. Newton draws a one meter by one meter square in front of Einstein and stands in the middle of it. When Einstein uncovers his eyes, he sees Newton immediately and exclaims: Newton! I found you! You're hit!"

Newton smiles and says: "You didn't find me. You found a Newton over a square meter. You found Pascal".

### Headlines from a Mathematical World

*Poll Finds 2016 Candidates Neck and Neck.*

Mathematically Literate World: Poll Finds 2016 Predictions Futile and Absurd.

*Programming today is a race between software engineers striving to build bigger and better idiot-proof programs, and the Universe trying to produce bigger and better idiots. So far, the Universe is winning.*

Douglas Adams

*Nothing is easier than to assign Names, Signs, or Expressions to these Fluxions, and it is not difficult to compute and operate by means of such Signs. But it will be found much more difficult, to omit the Signs and yet retain in our Minds the things, which we suppose to be signified by them. To consider the Exponents, whether Geometrical, or Algebraical, or Fluxionary, is no difficult Matter. But to form a precise Idea of a third Velocity for instance, in itself and by itself, Hoc opus, hic labor. (...) To me it seems evident, that Measures and Signs are absolutely necessary, in order to conceive or reason about Velocities; and that, consequently, when we think to conceive the Velocities, simply and in themselves, we are deluded by vain Abstractions.*

George Berkeley

[about him:] *Tame at home and dominant among colleagues, joyful in mathematics and deadly serious in quarrels among mathematicians, he was the closest thing to a reincarnation of Alcibiades that the nineteenth-century Germany could produce not only in its enthusiastic energy in daring to extreme, but also as fierce fighting when he was cornered – Alcibiades by Phrygians, Cantor by ideas.*

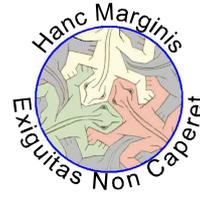
Georg Cantor

*Omnia apud me mathematica fiunt.* [With me everything turns into mathematics.]

René Descartes

*Imagination is more important than knowledge.*

Albert Einstein



|    |    |                                                                                                                                                |                                                                                                                                 |
|----|----|------------------------------------------------------------------------------------------------------------------------------------------------|---------------------------------------------------------------------------------------------------------------------------------|
| 1  | W  | (1640) Georg Mohr<br>(1776) Marie-Sophie Germain<br>(1895) Alexander Craig Aitken                                                              |                                                                                                                                 |
| 2  | T  | (1878) Edward Kasner<br>(1934) Paul Joseph Cohen                                                                                               |                                                                                                                                 |
| 3  | F  | (1835) John Howard Van Amringe<br>(1892) Hans Rademacher<br>(1900) Albert Edward Ingham<br>(1909) Stanislaw Marcin Ulam<br>(1971) Alice Riddle | RM171                                                                                                                           |
| 4  | S  | (1809) Benjamin Peirce<br>(1842) Francois Edouard Anatole Lucas<br>(1949) Shing-Tung Yau                                                       | RM123                                                                                                                           |
| 5  | S  | (1588) Thomas Hobbes<br>(1607) Honoré Fabri<br>(1622) Vincenzo Viviani<br>(1869) Sergi Alexeievich Chaplygin                                   |                                                                                                                                 |
| 15 | 6  | M                                                                                                                                              | (1801) William Hallowes Miller                                                                                                  |
|    | 7  | T                                                                                                                                              | (1768) François-Joseph Français                                                                                                 |
|    | 8  | W                                                                                                                                              | (1903) Marshall Harvey Stone                                                                                                    |
|    | 9  | T                                                                                                                                              | (1791) George Peacock<br>(1816) Charles Eugene Delaunay<br>(1894) Cypra Cecilia Krieger Dunaj<br>(1919) John Presper Heckert    |
|    | 10 | F                                                                                                                                              | (1857) Henry Ernest Dudeney                                                                                                     |
|    | 11 | S                                                                                                                                              | (1953) Andrew John Wiles                                                                                                        |
|    | 12 | S                                                                                                                                              | (1794) Germain Pierre Dandelin<br>(1852) Carl Louis Ferdinand von Lindemann<br>(1903) Jan Tinbergen                             |
| 16 | 13 | M                                                                                                                                              | (1728) Paolo Frisi<br>(1813) Duncan Farquharson Gregory<br>(1869) Ada Isabel Maddison<br>(1879) Francesco Severi                |
|    | 14 | T                                                                                                                                              | (1629) Christiaan Huygens                                                                                                       |
|    | 15 | W                                                                                                                                              | (1452) Leonardo da Vinci<br>(1548) Pietro Antonio Cataldi<br>(1707) Leonhard Euler<br>(1809) Herman Gunther Grassmann           |
|    | 16 | T                                                                                                                                              | (1682) John Hadley<br>(1823) Ferdinand Gotthold Max Eisenstein                                                                  |
|    | 17 | F                                                                                                                                              | (1798) Etienne Bobillier<br>(1853) Arthur Moritz Schonflies<br>(1863) Augustus Edward Hough Love                                |
|    | 18 | S                                                                                                                                              | (1791) Ottaviano Fabrizio Mossotti<br>(1907) Lars Valerian Ahlfors<br>(1918) Hsien Chung Wang<br>(1949) Charles Louis Fefferman |
|    | 19 | S                                                                                                                                              | (1880) Evgeny Evgenievich Slutsky<br>(1883) Richard von Mises<br>(1901) Kiyoshi Oka<br>(1905) Charles Ehresmann                 |
| 17 | 20 | M                                                                                                                                              | (1839) Francesco Siacchi                                                                                                        |
|    | 21 | T                                                                                                                                              | (1652) Michel Rolle<br>(1774) Jean Baptiste Biot<br>(1875) Teiji Takagi                                                         |
|    | 22 | W                                                                                                                                              | (1811) Otto Ludwig Hesse<br>(1887) Harald August Bohr<br>(1935) Bhami Srinivasan<br>(1939) Sir Michael Francis Atiyah           |
|    | 23 | T                                                                                                                                              | (1858) Max Karl Ernst Ludwig Planck<br>(1910) Sheila Scott Macintyre                                                            |
|    | 24 | F                                                                                                                                              | (1863) Giovanni Vailati<br>(1899) Oscar Zariski                                                                                 |
|    | 25 | S                                                                                                                                              | (1849) Felix Christian Klein<br>(1900) Wolfgang Pauli<br>(1903) Andrei Nicolayevich Kolmogorov                                  |
|    | 26 | S                                                                                                                                              | (1889) Ludwig Josef Johan Wittgenstein                                                                                          |
| 18 | 27 | M                                                                                                                                              | (1755) Marc-Antoine Parseval des Chenes<br>(1932) Gian-Carlo Rota                                                               |
|    | 28 | T                                                                                                                                              | (1906) Kurt Godel                                                                                                               |
|    | 29 | W                                                                                                                                              | (1854) Jules Henri Poincaré                                                                                                     |
|    | 30 | T                                                                                                                                              | (1777) Johann Carl Friedrich Gauss<br>(1916) Claude Elwood Shannon                                                              |

**Putnam 2000, A4**

Show that the improper integral

$$\lim_{B \rightarrow \infty} \int_0^B \sin(x) \sin(x^2) dx$$

converges.

**English Jokes that only intellectuals understand**

A Roman soldier walks in a bar asking for a Martinis.

“You mean Martini?” The bartender asks.

The Roman replies: “If I wanted a double, I would have asked for it!”

After some time, seeing a friend in the bar, the legionnaire holds up two fingers and says: “Five beers, please”.

**Headlines from a Mathematical World**

*One Dead in Shark Attack; See Tips for Shark Safety Inside.*

*Mathematically Literate World: One Dead in Tragic, Highly Unlikely Event; See Tips for Something Useful Inside.*

*There are some mysteries that the human mind will never penetrate. To be convinced we should not do anything else but throw a look at the tables of primes. We realize that there reigns no order or law. [1751]*

Leonhard Euler

*God does arithmetic.*

Johann Carl Friedrich Gauss

*Either mathematics is too big for the human mind or the human mind is more than a machine.*

Kurt Godel

*Geometry (which is the only science that it hath pleased God to bestow on mankind)...*

Thomas Hobbes

*Mathematics in general is fundamentally the science of self-evident things.*

Felix Christian Klein

*No mathematical research can be called real science if it can't be proven mathematically.*

Leonardo Da Vinci

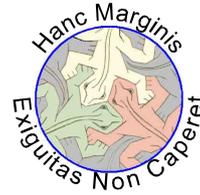
*[Arithmetic] can only be considered a science of suggestions, to which the principles and operations of algebra adapt, but by which are neither limited or determined.*

George Peacock

*There can never be surprises in logic.*

Ludwig Josef Johan Wittgenstein

|    |    |                                                                                          |                                                                                                                                            |                                                                        |       |
|----|----|------------------------------------------------------------------------------------------|--------------------------------------------------------------------------------------------------------------------------------------------|------------------------------------------------------------------------|-------|
| 1  | F  | (1825) Johann Jacob Balmer<br>(1908) Morris Kline<br>(1977) Maryam Mirzakhani            | RM122<br>RM189                                                                                                                             |                                                                        |       |
|    | 2  | S                                                                                        | (1860) D'Arcy Wentworth Thompson<br>(1905) Kazimierz Zarankiewicz                                                                          | RM138                                                                  |       |
|    | 3  | S                                                                                        | (1842) Otto Stolz<br>(1860) Vito Volterra<br>(1892) George Paget Thomson                                                                   | RM136<br>RM161                                                         |       |
| 19 | 4  | M                                                                                        | (1845) William Kingdon Clifford                                                                                                            |                                                                        |       |
|    | 5  | T                                                                                        | (1833) Lazarus Emmanuel Fuchs<br>(1883) Anna Johnson Pell Wheeler<br>(1897) Francesco Giacomo Tricomi<br>(1923) Cathleen Synge Morawetz    |                                                                        |       |
|    | 6  | W                                                                                        | (1872) Willem de Sitter<br>(1906) André Weil                                                                                               | RM088                                                                  |       |
|    | 7  | T                                                                                        | (1854) Giuseppe Veronese<br>(1881) Ebenezer Cunningham<br>(1896) Pavel Sergeievich Alexandrov<br>(1926) Alexis Claude Clairaut             |                                                                        |       |
|    | 8  | F                                                                                        | (1859) Johan Ludwig William Valdemar Jensen<br>(1905) Winifred Lydia Caunden Sargent                                                       |                                                                        |       |
|    | 9  | S                                                                                        | (1746) Gaspard Monge<br>(1876) Gilbert Ames Bliss<br>(1965) Karen Ellen Smith                                                              |                                                                        |       |
|    | 10 | S                                                                                        | (1788) Augustin Jean Fresnel<br>(1847) William Karl Joseph Killing<br>(1904) Edward James Mcshane<br>(1958) Piotr Rezierovich Silverbrahms |                                                                        |       |
|    | 20 | 11                                                                                       | M                                                                                                                                          | (1902) Edna Ernestine Kramer Lassar<br>(1918) Richard Phillips Feynman | RM076 |
|    | 12 | T                                                                                        | (1820) Florence Nightingale<br>(1845) Pierre René Jean Baptiste Henry Brocard<br>(1902) Frank Yates                                        | RM104                                                                  |       |
|    | 13 | W                                                                                        | (1750) Lorenzo Mascheroni<br>(1899) Pelageia Yakovlevna Polubarinova Kochina                                                               |                                                                        |       |
| 14 | T  | (1832) Rudolf Otto Sigismund Lipschitz<br>(1863) John Charles Fields                     | RM100                                                                                                                                      |                                                                        |       |
| 15 | F  | (1939) Brian Hartley<br>(1964) Sijue Wu                                                  |                                                                                                                                            |                                                                        |       |
| 16 | S  | (1718) Maria Gaetana Agnesi<br>(1821) Pafnuti Lvovi Chebyshev<br>(1911) John (Jack) Todd | RM112<br>RM139                                                                                                                             |                                                                        |       |
| 17 | S  | (1940) Alan Kay                                                                          |                                                                                                                                            |                                                                        |       |
| 21 | 18 | M                                                                                        | (1850) Oliver Heaviside<br>(1892) Bertrand Arthur William Russell                                                                          | RM160<br>RM052                                                         |       |
|    | 19 | T                                                                                        | (1865) Flora Philip<br>(1919) Georgii Dimitrievich Suvorov                                                                                 |                                                                        |       |
|    | 20 | W                                                                                        | (1861) Henry Seely White                                                                                                                   |                                                                        |       |
|    | 21 | T                                                                                        | (1471) Albrecht Dürer<br>(1792) Gustave Gaspard de Coriolis                                                                                | RM124                                                                  |       |
|    | 22 | F                                                                                        | (1865) Alfred Cardew Dixon                                                                                                                 |                                                                        |       |
|    | 23 | S                                                                                        | (1914) Lipa Bers                                                                                                                           | RM148                                                                  |       |
|    | 24 | S                                                                                        | (1544) William Gilbert                                                                                                                     |                                                                        |       |
|    | 22 | 25                                                                                       | M                                                                                                                                          | (1838) Karl Mikailovich Peterson                                       |       |
|    | 26 | T                                                                                        | (1667) Abraham de Moivre<br>(1896) Yuri Dimitrievich Sokolov                                                                               |                                                                        |       |
|    | 27 | W                                                                                        | (1862) John Edward Campbell                                                                                                                |                                                                        |       |
| 28 | T  | (1676) Jacopo Francesco Riccati<br>(1710) Johann (II) Bernoulli                          | RM093                                                                                                                                      |                                                                        |       |
| 29 | F  | (1882) Harry Bateman                                                                     |                                                                                                                                            |                                                                        |       |
| 30 | S  | (1814) Eugene Charles Catalan                                                            | RM184                                                                                                                                      |                                                                        |       |
| 31 | S  | (1926) John Kemeny                                                                       |                                                                                                                                            |                                                                        |       |



**Putnam 2000, A5**

Three distinct points with integer coordinates lie in the plane on a circle of radius  $r > 0$ . Show that two of these points are separated by a distance of at least  $r^{1/3}$ .

**English Jokes that only intellectuals understand**

Entropy isn't what it used to be.

**Headlines from a Mathematical World**

*Market Share for Electric Cars Triples.*

Mathematically Literate World: Market Share for Electric Cars Rises to 0.4%.

*A great deal more is known than has been proved.*

Richard Phillips Feynman

*When using a mathematical model, we must pay particular attention to the uncertainties of the model.*

Richard Phillips Feynman

*Universities hire professors the way some men choose wives – they want the ones the others will admire.*

Morris Kline

*How dare we speak of the laws of chance? Is this not the antithesis of all laws?*

Bertrand Arthur William Russell

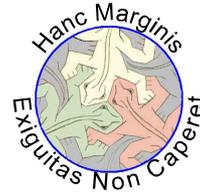
*Cells and tissues, bones and shells, leaves and flowers, are simply various portions of matter, and it is in obedience to the laws of physics that their particles have been moved, modelled and standardized. No exceptions to the rule that God always geometrizes. Their shape problems are primarily mathematical problems, growth problems are essentially physical problems, and the morphologist is ipso facto a student of the physical sciences.*

D'Arcy Wentworth Thompson

*Nothing is more fruitful, all mathematicians know, than those vague analogies, those dark reflections that lead from one theory to another, those furtive caresses, those inexplicable discrepancies: nothing gives a greater pleasure to the researcher.*

André Weil

|    |    |   |                                                                                                                                                                        |                |
|----|----|---|------------------------------------------------------------------------------------------------------------------------------------------------------------------------|----------------|
| 23 | 1  | M | (1796) Sadi Leonard Nicolas Carnot<br>(1851) Edward Bailey Elliott<br>(1899) Edward Charles Titchmarsh                                                                 |                |
|    | 2  | T | (1895) Tibor Radó                                                                                                                                                      |                |
|    | 3  | W | (1659) David Gregory                                                                                                                                                   |                |
|    | 4  | T | (1809) John Henry Pratt<br>(1966) Svetlana Yakovlevna Jitomirskaya                                                                                                     |                |
|    | 5  | F | (1814) Pierre Laurent Wantzel<br>(1819) John Couch Adams<br>(1883) John Maynard Keynes                                                                                 | RM065          |
|    | 6  | S | (1436) Johann Muller Regiomontanus<br>(1857) Aleksandr Michailovitch Lyapunov<br>(1906) Max Zorn                                                                       | RM185<br>RM077 |
|    | 7  | S | (1863) Edward Burr Van Vleck                                                                                                                                           |                |
| 24 | 8  | M | (1625) Giovanni Domenico Cassini<br>(1858) Charlotte Angus Scott<br>(1860) Alicia Boole Stott<br>(1896) Eleanor Pairman<br>(1923) Gloria Olive<br>(1924) Samuel Karlin |                |
|    | 9  | T | (1885) John Edensor Littlewood                                                                                                                                         | RM049          |
|    | 10 | W | (940) Mohammad Abu'L Wafa Al-Buzjani<br>(1887) Vladimir Ivanovich Smirnov                                                                                              | RM101          |
|    | 11 | T | (1881) Hilda Phoebe Hudson<br>(1937) David Bryant Mumford                                                                                                              |                |
|    | 12 | F | (1888) Zygmunt Janyszewski<br>(1937) Vladimir Igorevich Arnold                                                                                                         |                |
|    | 13 | S | (1831) James Clerk Maxwell<br>(1872) Jessie Chrystal Macmillan<br>(1876) William Sealey Gosset (Student)<br>(1928) John Forbes Nash                                    | RM113<br>RM149 |
|    | 14 | S | (1736) Charles Augustin de Coulomb<br>(1856) Andrei Andreyevich Markov<br>(1903) Alonzo Church                                                                         | RM125          |
| 25 | 15 | M | (1640) Bernard Lamy<br>(1894) Nikolai Gregorievich Chebotaryov                                                                                                         |                |
|    | 16 | T | (1915) John Wilder Tukey                                                                                                                                               |                |
|    | 17 | W | (1898) Maurits Cornelius Escher                                                                                                                                        | RM097          |
|    | 18 | T | (1858) Andrew Russell Forsyth<br>(1884) Charles Ernest Weatherburn<br>(1884) Frieda Nugel<br>(1913) Paul Teichmueller<br>(1915) Alice Turner Schafer                   | RM148          |
|    | 19 | F | (1623) Blaise Pascal<br>(1902) Wallace John Eckert                                                                                                                     | RM053          |
|    | 20 | S | (1873) Alfred Loewy<br>(1917) Helena Rasiowa                                                                                                                           |                |
|    | 21 | S | (1781) Simeon Denis Poisson<br>(1828) Giuseppe Bruno<br>(1870) Maria Skłodowska Curie                                                                                  | RM182          |
| 26 | 22 | M | (1822) Mario Pieri<br>(1864) Hermann Minkowsky<br>(1910) Konrad Zuse<br>(1932) Mary Wynne Warner                                                                       |                |
|    | 23 | T | (1912) Alan Mathison Turing                                                                                                                                            | RM089          |
|    | 24 | W | (1880) Oswald Veblen                                                                                                                                                   |                |
|    | 25 | T | (1908) William Van Orman Quine                                                                                                                                         |                |
|    | 26 | F | (1823) William Thomson, Lord Kelvin<br>(1918) Yudell Leo Luke                                                                                                          | RM161          |
|    | 27 | S | (1806) Augustus de Morgan                                                                                                                                              |                |
|    | 28 | S | (1875) Henri Leon Lebesgue                                                                                                                                             | RM173          |
| 27 | 29 | M | (1888) Aleksandr Aleksandrovich Friedmann<br>(1979) Artur Avila Cordeiro de Melo                                                                                       | RM101<br>RM189 |
|    | 30 | T | (1791) Felix Savart<br>(1958) Abigail A Thompson                                                                                                                       |                |



**Putnam 2000, A6**

Be  $f(x)$  a polynomial with integer coefficients. Define a sequence of integers  $a_0, a_1, \dots$  such that  $a_0 = 0$  and  $a_{n+1} = f(a_n)$ . Prove that if there exists a positive integer  $m$  for which  $a_m = 0$ , then either  $a_1 = 0$  or  $a_2 = 0$ .

**English Jokes that only intellectuals understand**

Werner Heisenberg, Kurt Gödel and Noam Chomsky walk into a bar. Heisenberg turns to the other two and says: "Clearly this is a joke, but how we figure out if it's funny or not?".

Gödel replies: "We don't know that because we're inside the joke". Chomsky says: "Of course it's funny. You're just telling it wrong".

**Headlines from a Mathematical World**

*Still No Scientific Consensus on Global Warming.*

Mathematically Literate World: Still 90% Scientific Consensus on Global Warming.

*The motto that I would adopt against a path designed to stop the progress of the discoveries would be "remember square root of -1"*

Augustus De Morgan

*A distinctive feature of mathematics is that it does not use all those long and difficult names like the other sciences. Indeed, it is more conservative than other sciences, as it clings tenaciously to the old terms.*

E. Kasner, J.R. Newman

*Perhaps the greatest paradox is that there are paradoxes in mathematics.*

E. Kasner, J.R. Newman

*It has been pointed out already that no knowledge of probabilities, less in degree than certainty, helps us to know what conclusions are true, and that there is no direct relation between the truth of a proposition and its probability. Probability begins and ends with probability.*

John Maynard Keynes

*In passing, I firmly believe that research should be offset by a certain amount of teaching, if only as a change from the agony of research. The trouble, however, I freely admit, is that in practice you get either no teaching, or else far too much.*

John Edensor Littlewood

*I read in the proof sheets of Hardy on Ramanujan: "As someone said, each of the positive integers was one of his personal friends." My reaction was, "I wonder who said that; I wish I had." In the next proof-sheets I read (what now stands), "It was Littlewood who said..."*

John Edensor Littlewood

|    |    |                                                                                                               |                                                                                                                                    |
|----|----|---------------------------------------------------------------------------------------------------------------|------------------------------------------------------------------------------------------------------------------------------------|
| 1  | W  | (1643) Gottfried Wilhelm von Leibniz<br>(1788) Jean Victor Poncelet<br>(1906) Jean Alexandre Eugène Dieudonné | RM054                                                                                                                              |
| 2  | T  | (1820) William John Rankine<br>(1852) William Burnside<br>(1925) Olga Arsen'evna Oleinik                      |                                                                                                                                    |
| 3  | F  | (1807) Ernest Jean Philippe Fauque de Jonquiere<br>(1897) Jesse Douglas                                       | RM162                                                                                                                              |
| 4  | S  | (1906) Daniel Edwin Rutherford<br>(1917) Michail Samoilovich Livsic                                           |                                                                                                                                    |
| 5  | S  | (1936) James Mirrlees                                                                                         |                                                                                                                                    |
| 28 | 6  | M                                                                                                             | (1849) Alfred Bray Kempe                                                                                                           |
|    | 7  | T                                                                                                             | (1816) Johann Rudolf Wolf<br>(1906) William Feller<br>(1922) Vladimir Aleksandrovich Marchenko                                     |
|    | 8  | W                                                                                                             | (1760) Christian Kramp<br>(1904) Henri Paul Cartan                                                                                 |
|    | 9  | T                                                                                                             | (1845) George Howard Darwin<br>(1931) Valentina Mikhailovna Borok                                                                  |
|    | 10 | F                                                                                                             | (1856) Nikola Tesla<br>(1862) Roger Cotes<br>(1868) Oliver Dimon Kellogg                                                           |
|    | 11 | S                                                                                                             | (1857) Sir Joseph Larmor<br>(1888) Jacob David Tamarkin<br>(1890) Giacomo Albanese                                                 |
|    | 12 | S                                                                                                             | (1875) Ernest Sigismund Fischer<br>(1895) Richard Buckminster Fuller<br>(1935) Nicolas Bourbaki                                    |
| 29 | 13 | M                                                                                                             | (1527) John Dee<br>(1741) Karl Friedrich Hindenburg                                                                                |
|    | 14 | T                                                                                                             | (1671) Jacques D'Allonville<br>(1793) George Green                                                                                 |
|    | 15 | W                                                                                                             | (1865) Wilhelm Wirtinger<br>(1898) Mary Taylor Slow<br>(1906) Adolph Andrej Pavlovich Yushkevich                                   |
|    | 16 | T                                                                                                             | (1678) Jakob Hermann<br>(1903) Irmgard Flugge-Lotz                                                                                 |
|    | 17 | F                                                                                                             | (1831) Victor Mayer Amedèe Mannheim<br>(1837) Wilhelm Lexis<br>(1944) Krystyna Maria Trybulec Kuperberg                            |
|    | 18 | S                                                                                                             | (1013) Hermann von Reichenau<br>(1635) Robert Hooke<br>(1853) Hendrik Antoon Lorentz                                               |
|    | 19 | S                                                                                                             | (1768) Francois Joseph Servois                                                                                                     |
| 30 | 20 | M                                                                                                             | (1876) Otto Blumenthal<br>(1947) Gerd Binnig                                                                                       |
|    | 21 | T                                                                                                             | (1620) Jean Picard<br>(1848) Emil Weyr<br>(1849) Robert Simpson Woodward<br>(1861) Herbert Ellsworth Slaughter                     |
|    | 22 | W                                                                                                             | (1784) Friedrich Wilhelm Bessel                                                                                                    |
|    | 23 | T                                                                                                             | (1775) Etienne Louis Malus<br>(1854) Ivan Slezynsky                                                                                |
|    | 24 | F                                                                                                             | (1851) Friedrich Herman Schottky<br>(1871) Paul Epstein<br>(1923) Christine Mary Hamill                                            |
|    | 25 | S                                                                                                             | (1808) Johann Benedict Listing                                                                                                     |
|    | 26 | S                                                                                                             | (1903) Kurt Mahler                                                                                                                 |
| 31 | 27 | M                                                                                                             | (1667) Johann Bernoulli<br>(1801) George Biddel Airy<br>(1848) Lorand Baron von Eötvös<br>(1871) Ernst Friedrich Ferdinand Zermelo |
|    | 28 | T                                                                                                             | (1954) Gerd Faltings                                                                                                               |
|    | 29 | W                                                                                                             | (1898) Isidor Isaac Rabi                                                                                                           |
|    | 30 | T                                                                                                             | (1889) Vladimir Kosma Zworokyn                                                                                                     |
|    | 31 | F                                                                                                             | (1704) Gabriel Cramer<br>(1712) Johann Samuel Koenig<br>(1926) Hilary Putnam                                                       |



**Putnam 2000, B1**

Let  $a_j, b_j, c_j$  be integers for  $1 \leq j \leq N$ . Assume for each  $j$ , at least one of  $a_j, b_j, c_j$  is odd. Show that there exists integers  $r, s, t$  such that  $r a_j + s b_j + t c_j$  is odd for at least  $4N/7$  values of  $j$ .

**English Jokes that only intellectuals understand**

Pavlov is sitting at a pub enjoying a pint, the phone rings and he jumps out shouting: "Oh shit, I forgot to feed the dog!"

**Headlines from a Mathematical World**

*Economist: "Eliminate Minimum Wage to Create Jobs, Improve Economy".*

*Mathematically Literate World: Economist: "Eliminate Minimum Wage, then Pray Our Model Has Some Basis in Reality".*

*Historically speaking, it is clearly false that mathematics is free of contradictions. The non-contradiction seems more an objective to be achieved than a quality given by God once and for all. There is no well-defined demarcation between the contradictions that occur daily in the work of any mathematician – novice or master they all make mistakes more or less easy to find – and the paradoxes of greatest importance providing bread for the teeth of logics for decades and, in certain cases, for centuries.*

Nicolas Bourbaki

*We believe in the reality of mathematics, but of course when philosophers attack us with their paradoxes we rush to take shelter behind formalism and say: "Mathematics is just a combination of meaningless symbols" and pull out the chapters 1 and 2 of set theory. When you finally leave us in peace, we return to our mathematics and do as we always have, trying the feeling (that every mathematical experiences) to work with something real. Feeling that is probably an illusion, but very comfortable. This is the attitude of Bourbaki against the fundamentals.*

Jean Alexandre Eugène Dieudonné

*He who understands Archimedes and Apollonius will admire less the achievements of the foremost men of later times.*

Gottfried Wilhelm von Leibniz

*The art of discovering the causes of phenomena, or true hypothesis, is like the art of deciphering, in which an ingenious conjecture greatly shortens the road.*

Gottfried Wilhelm von Leibniz

*Mathematics honours the human spirit.*

Gottfried Wilhelm von Leibniz

|    |    |                                                                                     |                                                                                                                                                     |
|----|----|-------------------------------------------------------------------------------------|-----------------------------------------------------------------------------------------------------------------------------------------------------|
| 1  | S  | (1861) Ivar Otto Bendixson<br>(1881) Otto Toeplitz<br>(1955) Bernadette Perrin-Riou |                                                                                                                                                     |
| 2  | S  | (1856) Ferdinand Rudio<br>(1902) Mina Spiegel Rees                                  |                                                                                                                                                     |
| 32 | 3  | M                                                                                   | (1914) Mark Kac<br>RM115                                                                                                                            |
|    | 4  | T                                                                                   | (1805) Sir William Rowan Hamilton<br>(1838) John Venn<br>RM079                                                                                      |
|    | 5  | W                                                                                   | (1802) Niels Henrik Abel<br>(1941) Alexander Keewatin Dewdney<br>RM055                                                                              |
|    | 6  | T                                                                                   | (1638) Nicolas Malebranche<br>(1741) John Wilson                                                                                                    |
|    | 7  | F                                                                                   | (1868) Ladislaus Josephowitsch Bortkiewitz                                                                                                          |
|    | 8  | S                                                                                   | (1902) Paul Adrien Maurice Dirac<br>(1931) Sir Roger Penrose<br>(1974) Manjul Bhargava<br>RM103                                                     |
|    | 9  | S                                                                                   | (1537) Francesco Barozzi (Franciscus Barocius)<br>(1940) Linda Goldway Keen<br>RM189                                                                |
| 33 | 10 | M                                                                                   | (1602) Gilles Personne de Roberval<br>(1926) Carol Ruth Karp                                                                                        |
|    | 11 | T                                                                                   | (1730) Charles Bossut<br>(1842) Enrico D'Ovidio                                                                                                     |
|    | 12 | W                                                                                   | (1882) Jules Antoine Richard<br>(1887) Erwin Rudolf Josef Alexander Schrödinger<br>RM103                                                            |
|    | 13 | T                                                                                   | (1625) Erasmus Bartholin<br>(1819) George Gabriel Stokes<br>(1861) Cesare Burali-Forti<br>RM187                                                     |
|    | 14 | F                                                                                   | (1530) Giovanni Battista Benedetti<br>(1842) Jean Gaston Darboux<br>(1865) Guido Castelnuovo<br>(1866) Charles Gustave Nicolas de La Vallée-Poussin |
|    | 15 | S                                                                                   | (1863) Aleksei Nikolaevich Krylov<br>(1892) Louis Pierre Victor Duc de Broglie<br>(1901) Piotr Sergeevich Novikov<br>RM175                          |
|    | 16 | S                                                                                   | (1773) Louis-Benjamin Francoeur<br>(1821) Arthur Cayley                                                                                             |
| 34 | 17 | M                                                                                   | (1601) Pierre de Fermat<br>RM091                                                                                                                    |
|    | 18 | T                                                                                   | (1685) Brook Taylor                                                                                                                                 |
|    | 19 | W                                                                                   | (1646) John Flamsteed<br>(1739) Georg Simon Klugel                                                                                                  |
|    | 20 | T                                                                                   | (1710) Thomas Simpson<br>(1863) Corrado Segre<br>(1882) Wacław Sierpiński                                                                           |
|    | 21 | F                                                                                   | (1789) Augustin Louis Cauchy<br>RM127                                                                                                               |
|    | 22 | S                                                                                   | (1647) Denis Papin                                                                                                                                  |
|    | 23 | S                                                                                   | (1683) Giovanni Poleni<br>(1829) Moritz Benedikt Cantor<br>(1842) Osborne Reynolds                                                                  |
| 35 | 24 | M                                                                                   | (1561) Bartholomeo Pitiscus<br>(1942) Karen Keskulla Uhlenbeck<br>RM163                                                                             |
|    | 25 | T                                                                                   | (1561) Philip Van Lansberge<br>(1844) Thomas Muir                                                                                                   |
|    | 26 | W                                                                                   | (1728) Johann Heinrich Lambert<br>(1875) Giuseppe Vitali<br>(1965) Marcus Peter Francis du Sautoy                                                   |
|    | 27 | T                                                                                   | (1858) Giuseppe Peano<br>RM067                                                                                                                      |
|    | 28 | F                                                                                   | (1862) Roberto Marcolongo<br>(1796) Irénée Jules Bienaymé<br>RM187                                                                                  |
|    | 29 | S                                                                                   | (1904) Leonard Roth                                                                                                                                 |
|    | 30 | S                                                                                   | (1703) Giovanni Ludovico Calandrini<br>(1856) Carle David Tolmé Runge<br>(1906) Olga Taussky-Todd<br>RM186<br>RM139                                 |
| 36 | 31 | M                                                                                   | (1821) Hermann Ludwig Ferdinand von Helmholtz<br>(1885) Herbert Westren Turnbull                                                                    |



**Putnam 2000, B2**

Prove that the expression:

$$\frac{\gcd(m,n)}{n} \binom{n}{m}$$

is an integer for all pairs of integers  $n \geq m \geq 1$ .

**English Jokes that only intellectuals understand**

Helium walks in the bar and orders a beer, the bartender says: "Sorry, we don't serve Noble Gases here". He doesn't react.

**Headlines from a Mathematical World**

*Illegal Downloaders Would Have Spent \$300 Million to Obtain Same Music Legally.*

Mathematically Literate World: Illegal Downloaders Probably Would Not Have Bothered to Obtain Same Music Legally.

*It appears to me that if one wishes to make progress in mathematics, one should study the masters and not the pupils.*

Niels Henrik Abel

*Mathematics is the tool especially suited for dealing with abstract concepts of any kind and there is no limit to its power in this field.*

Paul Adrien Maurice Dirac

*A book on the new physics, if it's not a pure description of experimental work, must be essentially mathematical.*

Paul Adrien Maurice Dirac

*A beautiful idea is much more likely to be right than an ugly idea.*

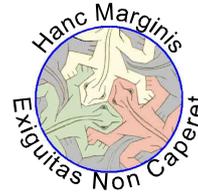
Sir Roger Penrose

*The notion of mathematical truth goes beyond the whole concept of formalism. In the mathematical truth there is something absolute and 'divine'.*

Sir Roger Penrose

*There is nothing that stimulates the creative process of a mathematician as the thought of immortality that gives the fact of having your name associated with a theorem.*

Marcus Peter Francis Du Sautoy



|    |    |                                                                                               |                                                                                                                                                              |                         |
|----|----|-----------------------------------------------------------------------------------------------|--------------------------------------------------------------------------------------------------------------------------------------------------------------|-------------------------|
| 1  | T  | (1659) Joseph Saurin<br>(1835) William Stanley Jevons                                         |                                                                                                                                                              |                         |
| 2  | W  | (1878) Mauriche René Frechet<br>(1923) René Thom                                              | RM080                                                                                                                                                        |                         |
| 3  | T  | (1814) James Joseph Sylvester<br>(1884) Solomon Lefschetz<br>(1908) Lev Semenovich Pontryagin | RM104                                                                                                                                                        |                         |
| 4  | F  | (1809) Luigi Federico Menabrea                                                                | RM150                                                                                                                                                        |                         |
| 5  | S  | (1667) Giovanni Girolamo Saccheri<br>(1725) Jean Etienne Montucla                             | RM128                                                                                                                                                        |                         |
| 6  | S  | (1859) Boris Jakovlevich Bukreev<br>(1863) Dimitri Aleksandrovich Grave                       |                                                                                                                                                              |                         |
| 37 | 7  | M                                                                                             | (1707) George Louis Leclerc Comte de Buffon<br>(1948) Cheryl Elisabeth Praeger<br>(1955) Efim Zelmanov                                                       |                         |
|    | 8  | T                                                                                             | (1584) Gregorius Saint-Vincent<br>(1588) Marin Mersenne                                                                                                      | RM092                   |
|    | 9  | W                                                                                             | (1860) Frank Morley<br>(1914) Marjorie Lee Browne                                                                                                            |                         |
|    | 10 | T                                                                                             | (1839) Charles Sanders Peirce                                                                                                                                | RM123                   |
|    | 11 | F                                                                                             | (1623) Stefano degli Angeli<br>(1798) Franz Ernst Neumann<br>(1877) Sir James Hopwood Jeans                                                                  |                         |
|    | 12 | S                                                                                             | (1891) Antoine André Louis Reynaud<br>(1900) Haskell Brooks Curry<br>(1894) Dorothy Maud Wrinch                                                              |                         |
|    | 13 | S                                                                                             | (1873) Constantin Carathéodory<br>(1885) Wilhelm Johann Eugen Blaschke                                                                                       |                         |
| 38 | 14 | M                                                                                             | (1858) Henry Burchard Fine<br>(1891) Ivan Matveevich Vinogradov                                                                                              |                         |
|    | 15 | T                                                                                             | (973) Abu Arrayhan Muhammad Ibn Ahmad Al'Biruni<br>(1886) Paul Pierre Levy                                                                                   | RM164                   |
|    | 16 | W                                                                                             | (1494) Francisco Maurolico<br>(1736) Johann Nikolaus Tetens                                                                                                  |                         |
|    | 17 | T                                                                                             | (1743) Marie Jean Antoine Nicolas de Caritat de Condorcet<br>(1826) Georg Friedrich Bernhard Riemann                                                         | RM176<br>RM068          |
|    | 18 | F                                                                                             | (1752) Adrien Marie Legendre                                                                                                                                 | RM140                   |
|    | 19 | S                                                                                             | (1749) Jean Baptiste Delambre                                                                                                                                |                         |
|    | 20 | S                                                                                             | (1842) Alexander Wilhelm von Brill<br>(1861) Frank Nelson Cole                                                                                               |                         |
| 39 | 21 | M                                                                                             | (1899) Juliusz Pawel Schauder<br>(1917) Phyllis Nicolson                                                                                                     |                         |
|    | 22 | T                                                                                             | (1765) Paolo Ruffini<br>(1769) Louis Puissant<br>(1803) Jaques Charles Francois Sturm                                                                        | RM116                   |
|    | 23 | W                                                                                             | (1768) William Wallace<br>(1900) David Van Dantzig                                                                                                           |                         |
|    | 24 | T                                                                                             | (1501) Girolamo Cardano<br>(1625) Johan de Witt<br>(1801) Michail Vasilevich Ostrogradski<br>(1862) Winifred Edgerton Merrill<br>(1945) Ian Nicholas Stewart | RM064<br>RM188<br>RM056 |
|    | 25 | F                                                                                             | (1819) George Salmon<br>(1888) Stefan Mazurkiewicz                                                                                                           |                         |
|    | 26 | S                                                                                             | (1688) Willem Jakob 's Gravesande<br>(1854) Percy Alexander Macmahon<br>(1891) Hans Reichenbach                                                              |                         |
|    | 27 | S                                                                                             | (1855) Paul Émile Appell<br>(1876) Earle Raymond Hedrick<br>(1919) James Hardy Wilkinson                                                                     |                         |
| 40 | 28 | M                                                                                             | (1698) Pierre Louis Moreau de Maupertuis<br>(1761) Ferdinand Francois Desirè Budan de Boislaurent<br>(1873) Julian Lowell Coolidge                           | RM152                   |
|    | 29 | T                                                                                             | (1561) Adriaan Van Roomen<br>(1812) Adolph Gopel                                                                                                             |                         |
|    | 30 | W                                                                                             | (1775) Robert Adrain<br>(1829) Joseph Wolstenholme<br>(1883) Ernst Hellinger                                                                                 |                         |

**Putnam 2000, B3**

Let  $f(t) = \sum_{j=1}^N a_j \sin(2\pi jt)$ , where each  $a_i$  is real and  $a_N \neq 0$ .

Let  $N_k$  denote the number of zeroes (including multiplicities) in  $[0, 1)$  of  $\frac{d^k f}{dt^k}$ . Prove that:

$$N_0 \leq N_1 \leq N_2 \dots \text{ and } \lim_{k \rightarrow \infty} N_k = 2N.$$

**English Jokes that only intellectuals understand**

Schrödinger's cat walks into a bar. And doesn't.

**Headlines from a Mathematical World**

*Market Rebounds after Assurances from Fed Chair.*

Mathematically Literate World: Market Rebounds after Regression to the Mean.

*Poincaré's point of view of phase space has proven to be so useful that today it can be found in every field of science - and in fields that are not at all scientific.*

Jack Cohen, Terry Pratchett, Ian Stewart

*Information is a useful concept, but it is curious that "To be or not to be" contains the same information according to Shannon, and less information according Chaitin, of "xyQGRIlfry & sk0wc\_% d". The reason for this disparity is that information is not the same thing as meaning. This is fascinating. What really matters to people is the meaning of a message, not the number of bits, but mathematicians have not been able to quantify the significance. For now.*

Jack Cohen, Terry Pratchett, Ian Stewart

*The strangest number in the multiverse is not infinite, but one.*

Jack Cohen, Terry Pratchett, Ian Stewart

*I think the probability theory is the only branch of mathematics in which good authors often get completely wrong results.*

Charles Sanders Peirce

*Time was when all the parts of the subject were dissevered, when algebra, geometry, and arithmetic either lived apart or kept up cold relations of acquaintance confined to occasional calls upon one another; but that is now at an end; they are drawn together and are constantly becoming more and more intimately related and connected by a thousand fresh ties, and we may confidently look forward to a time when they shall form but one body with one soul.*

James Joseph Sylvester

*The importance of the "New Mathematics" lies mainly in the fact that it has taught us the difference between the disc and the circle.*

René Thom

|    |    |                                                                                                                                                 |                                                                                                         |       |
|----|----|-------------------------------------------------------------------------------------------------------------------------------------------------|---------------------------------------------------------------------------------------------------------|-------|
| 1  | T  | (1671) Luigi Guido Grandi<br>(1898) Bela Kerekjarto'<br>(1912) Kathleen Timpson Ollerenshaw                                                     | RM177                                                                                                   |       |
| 2  | F  | (1825) John James Walker<br>(1908) Arthur Erdélyi                                                                                               |                                                                                                         |       |
| 3  | S  | (1944) Pierre René Deligne                                                                                                                      |                                                                                                         |       |
| 4  | S  | (1759) Louis Francois Antoine Arbogast<br>(1797) Jerome Savary                                                                                  |                                                                                                         |       |
| 41 | 5  | M                                                                                                                                               | (1732) Nevil Maskelyne<br>(1781) Bernhard Placidus Johann Nepomuk Bolzano<br>(1861) Thomas Little Heath | RM117 |
| 6  | T  | (1552) Matteo Ricci<br>(1831) Julius Wilhelm Richard Dedekind<br>(1908) Sergei Lvovich Sobolev                                                  | RM141<br>RM081                                                                                          |       |
| 7  | W  | (1885) Niels Bohr                                                                                                                               | RM063                                                                                                   |       |
| 8  | T  | (1908) Hans Arnold Heilbronn                                                                                                                    |                                                                                                         |       |
| 9  | F  | (1581) Claude Gaspard Bachet de Meziriac<br>(1704) Johann Andrea von Segner<br>(1873) Karl Schwarzschild<br>(1949) Fan Rong K Chung Graham      | RM153<br>RM110                                                                                          |       |
| 10 | S  | (1861) Heinrich Friedrich Karl Ludwig Burkhardt                                                                                                 |                                                                                                         |       |
| 11 | S  | (1675) Samuel Clarke<br>(1777) Barnabè Brisson<br>(1881) Lewis Fry Richardson<br>(1885) Alfred Haar<br>(1910) Cahit Arf                         |                                                                                                         |       |
| 42 | 12 | M                                                                                                                                               | (1860) Elmer Sperry                                                                                     |       |
| 13 | T  | (1890) Georg Feigl<br>(1893) Kurt Werner Friedrich Reidemeister<br>(1932) John Griggs Thomson                                                   |                                                                                                         |       |
| 14 | W  | (1687) Robert Simson<br>(1801) Joseph Antoine Ferdinand Plateau<br>(1868) Alessandro Padoa                                                      |                                                                                                         |       |
| 15 | T  | (1608) Evangelista Torricelli<br>(1735) Jesse Ramsden<br>(1776) Peter Barlow<br>(1931) Eléna Wexler-Kreindler                                   | RM165                                                                                                   |       |
| 16 | F  | (1879) Philip Edward Bertrand Jourdain                                                                                                          |                                                                                                         |       |
| 17 | S  | (1759) Jacob (II) Bernoulli<br>(1888) Paul Isaac Bernays                                                                                        | RM093                                                                                                   |       |
| 18 | S  | (1741) John Wilson<br>(1945) Margaret Dusa Waddington Mcduff                                                                                    |                                                                                                         |       |
| 43 | 19 | M                                                                                                                                               | (1903) Jean Frédéric Auguste Delsarte<br>(1910) Subrahmanyan Chandrasekhar                              | RM153 |
| 20 | T  | (1632) Sir Christopher Wren<br>(1863) William Henry Young<br>(1865) Aleksandr Petrovich Kotelnikov                                              | RM105                                                                                                   |       |
| 21 | W  | (1677) Nicolaus (I) Bernoulli<br>(1823) Enrico Betti<br>(1855) Giovan Battista Guccia<br>(1893) William Leonard Ferrar<br>(1914) Martin Gardner | RM093<br>RM150<br>RM129<br>RM137                                                                        |       |
| 22 | T  | (1587) Joachim Jungius<br>(1895) Rolf Herman Nevanlinna<br>(1907) Sarvadaman Chowla                                                             |                                                                                                         |       |
| 23 | F  | (1865) Piers Bohl                                                                                                                               |                                                                                                         |       |
| 24 | S  | (1804) Wilhelm Eduard Weber<br>(1873) Edmund Taylor Whittaker                                                                                   |                                                                                                         |       |
| 25 | S  | (1811) Évariste Galois                                                                                                                          | RM069                                                                                                   |       |
| 44 | 26 | M                                                                                                                                               | (1849) Ferdinand Georg Frobenius<br>(1857) Charles Max Mason<br>(1911) Shiing-Shen Chern                |       |
| 27 | T  | (1678) Pierre Remond de Montmort<br>(1856) Ernest William Hobson                                                                                |                                                                                                         |       |
| 28 | W  | (1804) Pierre François Verhulst                                                                                                                 |                                                                                                         |       |
| 29 | T  | (1925) Klaus Roth                                                                                                                               |                                                                                                         |       |
| 30 | F  | (1906) Andrej Nikolaevich Tichonov<br>(1946) William Paul Thurston                                                                              |                                                                                                         |       |
| 31 | S  | (1711) Laura Maria Catarina Bassi<br>(1815) Karl Theodor Wilhelm Weierstrass<br>(1935) Ronald Lewis Graham                                      | RM189<br>RM057<br>RM110                                                                                 |       |



**Putnam 2000, B4**

Let  $f(x)$  be a continuous function such that, for all  $x$ ,  $f(2x^2 - 1) = 2x f(x)$ . Show that  $f(x) = 0$  for  $-1 \leq x \leq 1$ .

**English Jokes that only intellectuals understand**

The programmer's wife tells him: "Run to the store and pick up a loaf of bread. If they have eggs, get a dozen".

The programmer comes home with 12 loaves of bread.

**Headlines from a Mathematical World**

*Rates of Cancer Approach Historic High.*

Mathematically Literate World: Rates of Surviving Long Enough to Develop Cancer Approach Historic High.

*If God creates a world of particles and waves, dancing in obedience to mathematical and physical laws, who are we to say that he cannot make use of those laws to cover the surface of a small planet with living creatures?*

Martin Gardner

*The lady said, "If I understand correctly, you're good with numbers." "No, I'm good with math," Randy replied. "Is it not what I said?" "Oh, no! The mathematicians are as far as possible from the real and specific numbers. We like to talk about numbers without actually being exposed to them: for that there are computers".*

Neal Stephenson

*What a fabulous way to save effort! For me, "134 divided 29" meant a tedious chore, while 134/29 was an object without implied work. Excited I went to my father to explain my great discovery; he told me that of course it was so, that a/b and a:b are simply synonyms. For him it was just a small change in notation.*

William Paul Thurston

*In things to be seen at once, much variety makes confusion, another vice of beauty. In things that are not seen at once, and have no respect one to another, great variety is commendable, provided this variety transgress not the rules of optics and geometry.*

Sir Christopher Wren

*Mathematics, among other things, teaches the persistence against the consequences, and rigor in following the path we have chosen arbitrarily.*

Paul Valéry

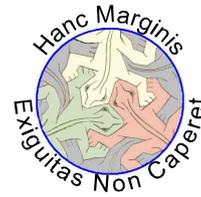
*Arithmetic is being able to count to twenty without taking off your shoes.*

Mickey Mouse

*He who can properly define and divide is to be considered a god.*

Plato

|    |    |                                                                                                                                                             |                                                                                                                                                                                                                                    |
|----|----|-------------------------------------------------------------------------------------------------------------------------------------------------------------|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| 1  | S  | (1535) Giambattista della Porta                                                                                                                             |                                                                                                                                                                                                                                    |
| 45 | 2  | M                                                                                                                                                           | (1815) George Boole<br>(1826) Henry John Stephen Smith<br>RM094                                                                                                                                                                    |
| 3  | T  | (1867) Martin Wilhelm Kutta<br>(1878) Arthur Byron Coble<br>(1896) Raymond Louis Wilder<br>(1906) Carl Benjamin Boyer                                       |                                                                                                                                                                                                                                    |
| 4  | W  | (1744) Johann (III) Bernoulli<br>(1865) Pierre Simon Girard<br>RM093                                                                                        |                                                                                                                                                                                                                                    |
| 5  | T  | (1848) James Whitbread Lee Glaisher<br>(1930) John Frank Adams                                                                                              |                                                                                                                                                                                                                                    |
| 6  | F  | (1781) Giovanni Antonio Amedeo Plana<br>(1906) Emma Markovna Trotskaia Lehmer<br>RM154                                                                      |                                                                                                                                                                                                                                    |
| 7  | S  | (1660) Thomas Fantet de Lagny<br>(1799) Karl Heinrich Graffe<br>(1567) Clara Immerwahr<br>(1898) Raphael Salem<br>RM182                                     |                                                                                                                                                                                                                                    |
| 8  | S  | (1656) Edmond Halley<br>(1846) Eugenio Bertini<br>(1848) Fredrich Ludwig Gottlob Frege<br>(1854) Johannes Robert Rydberg<br>(1869) Felix Hausdorff<br>RM190 |                                                                                                                                                                                                                                    |
| 46 | 9  | M                                                                                                                                                           | (1847) Carlo Alberto Castigliano<br>(1885) Theodor Franz Eduard Kaluza<br>(1885) Hermann Klaus Hugo Weyl<br>(1906) Jaroslav Borisovich Lopatynsky<br>(1913) Hedwig Eva Maria Kiesler (Hedy Lamarr)<br>(1922) Imre Lakatos<br>RM082 |
| 10 | T  | (1829) Helwin Bruno Christoffel                                                                                                                             |                                                                                                                                                                                                                                    |
| 11 | W  | (1904) John Henry Constantine Whitehead                                                                                                                     |                                                                                                                                                                                                                                    |
| 12 | T  | (1825) Michail Egorovich Vashchenko-Zakharchenko<br>(1842) John William Strutt Lord Rayleigh<br>(1927) Yutaka Taniyama                                      |                                                                                                                                                                                                                                    |
| 13 | F  | (1876) Ernest Julius Wilkzynsky<br>(1878) Max Wilhelm Dehn                                                                                                  |                                                                                                                                                                                                                                    |
| 14 | S  | (1845) Ulisse Dini<br>(1919) Paulette Libermann<br>(1975) Martin Hairer<br>RM189                                                                            |                                                                                                                                                                                                                                    |
| 15 | S  | (1688) Louis Bertrand Castel<br>(1793) Michel Chasles<br>(1794) Franz Adolph Taurinus                                                                       |                                                                                                                                                                                                                                    |
| 47 | 16 | M                                                                                                                                                           | (1835) Eugenio Beltrami<br>RM150                                                                                                                                                                                                   |
| 17 | T  | (1597) Henry Gellibrand<br>(1717) Jean Le Rond D'Alembert<br>(1790) August Ferdinand Möbius<br>RM166<br>RM118                                               |                                                                                                                                                                                                                                    |
| 18 | W  | (1872) Giovanni Enrico Eugenio Vacca<br>(1927) Jon Leslie Britton                                                                                           |                                                                                                                                                                                                                                    |
| 19 | T  | (1894) Heinz Hopf<br>(1900) Michail Alekseevich Lavrentev<br>(1901) Nina Karlovna Bari                                                                      |                                                                                                                                                                                                                                    |
| 20 | F  | (1889) Edwin Powell Hubble<br>(1924) Benoît Mandelbrot<br>(1963) William Timothy Gowers                                                                     |                                                                                                                                                                                                                                    |
| 21 | S  | (1867) Dimitri Sintsov                                                                                                                                      |                                                                                                                                                                                                                                    |
| 22 | S  | (1803) Giusto Bellavitis<br>(1840) Émile Michel Hyacinthe Lemoine                                                                                           |                                                                                                                                                                                                                                    |
| 48 | 23 | M                                                                                                                                                           | (1616) John Wallis<br>(1820) Issac Todhunter<br>(1917) Elizabeth Leonard Scott<br>RM070<br>RM106                                                                                                                                   |
| 24 | T  | (1549) Duncan Maclaren Young Sommerville<br>(1909) Gerhard Gentzen                                                                                          |                                                                                                                                                                                                                                    |
| 25 | W  | (1841) Fredrich Wilhelm Karl Ernst Schröder<br>(1873) Claude Louis Mathieu<br>(1943) Evelyn Merle Roden Nelson                                              |                                                                                                                                                                                                                                    |
| 26 | T  | (1894) Norbert Wiener<br>(1946) Enrico Bombieri<br>RM172                                                                                                    |                                                                                                                                                                                                                                    |
| 27 | F  | (1867) Arthur Lee Dixon                                                                                                                                     |                                                                                                                                                                                                                                    |
| 28 | S  | (1898) John Wishart                                                                                                                                         |                                                                                                                                                                                                                                    |
| 29 | S  | (1803) Christian Andreas Doppler<br>(1849) Horace Lamb<br>(1879) Nikolay Mitrofanovich Krylov                                                               |                                                                                                                                                                                                                                    |
| 49 | 30 | M                                                                                                                                                           | (1549) Sir Henry Savile<br>(1969) Matilde Marcolli<br>RM142                                                                                                                                                                        |



**Putnam 2000, B5**

Let  $S_0$  be a finite set of positive integers. We define finite sets  $S_1, S_2, \dots$  of positive integers as follows: the integer  $a$  is in  $S_{n+1}$  if and only if exactly one of  $a-1$  and  $a$  is in  $S_n$ . Show that there exist infinitely many integers  $N$  for which  $S_N = S_0 \cup \{N+a : a \in S_0\}$ .

**English Jokes that only intellectuals understand**

A logician's wife is having a baby. The doctor immediately hands the newborn to the dad.

His wife asks impatiently: "So, is it a boy or a girl?"

The logician replies: "Yes".

**Headlines from a Mathematical World**

*Unemployment Rate Jumps from 7.6% to 7.8%.*

Mathematically Literate World: Unemployment Rate Probably a Little Under 8%; Maybe Rising, or Not, Can't Really Tell.

*Neither in the subjective nor in the objective world can we find a criterion for the reality of the number concept, because the first contains no such concept, and the second contains nothing that is free from the concept. How then can we arrive at a criterion? Not by evidence, for the dice of evidence are loaded. Not by logic, for logic has no existence independent of mathematics: it is only one phase of this multiplied necessity that we call mathematics. How then shall mathematical concepts be judged? They shall not be judged. Mathematics is the supreme arbiter. From its decisions there is no appeal. We cannot change the rules of the game, we cannot ascertain whether the game is fair. We can only study the player at his game; not, however, with the detached attitude of a bystander, for we are watching our own minds at play.*

George Dantzig

*Here's another good reason why the models shall be as simple as possible: if we're lucky, we can use the same model to study many different phenomena at once.*

William Timothy Gowers

*[Arithmetic] is one of the oldest branches, perhaps the very oldest branch, of human knowledge; and yet some of its most abstruse secrets lie close to its tritest truths.*

Henry John Stephen Smith

*...numbers have neither substance, nor meaning, nor qualities. They are nothing but marks, and all that is in them we have put into them by the simple rule of straight succession..*

Hermann Klaus Hugo Weyl

*One of the chief duties of a mathematician in acting as an advisor to scientists is to discourage them from expecting too much of mathematicians.*

Norbert Wiener

|    |    |                                                                                                                                                       |                                                                                                                                |                |
|----|----|-------------------------------------------------------------------------------------------------------------------------------------------------------|--------------------------------------------------------------------------------------------------------------------------------|----------------|
| 1  | T  | (1792) Nikolay Yvanovich Lobachevsky<br>(1847) Christine Ladd-Franklin                                                                                | RM083                                                                                                                          |                |
| 2  | W  | (1831) Paul David Gustav du Bois-Reymond<br>(1901) George Frederick James Temple                                                                      |                                                                                                                                |                |
| 3  | T  | (1903) Sidney Goldstein<br>(1924) John Backus                                                                                                         |                                                                                                                                |                |
| 4  | F  | (1795) Thomas Carlyle                                                                                                                                 |                                                                                                                                |                |
| 5  | S  | (1868) Arnold Johannes Wilhelm Sommerfeld<br>(1901) Werner Karl Heisenberg<br>(1907) Giuseppe Occhialini                                              | RM155<br>RM122                                                                                                                 |                |
| 6  | S  | (1682) Giulio Carlo Fagnano dei Toschi                                                                                                                |                                                                                                                                |                |
| 50 | 7  | M                                                                                                                                                     | (1647) Giovanni Ceva<br>(1823) Leopold Kronecker<br>(1830) Antonio Luigi Gaudenzio Giuseppe Cremona<br>(1924) Mary Ellen Rudin | RM150          |
| 8  | T  | (1508) Regnier Gemma Frisius<br>(1865) Jaques Salomon Hadamard<br>(1919) Julia Bowman Robinson                                                        |                                                                                                                                |                |
| 9  | W  | (1883) Nikolai Nikolaievich Luzin<br>(1906) Grace Brewster Murray Hopper<br>(1917) Sergei Vasilovich Fomin                                            |                                                                                                                                |                |
| 10 | T  | (1804) Karl Gustav Jacob Jacobi<br>(1815) Augusta Ada King Countess Of Lovelace                                                                       | RM059                                                                                                                          |                |
| 11 | F  | (1882) Max Born                                                                                                                                       | RM155                                                                                                                          |                |
| 12 | S  | (1832) Peter Ludwig Mejdell Sylov<br>(1913) Emma Castelnuovo                                                                                          | RM191                                                                                                                          |                |
| 13 | S  | (1724) Franz Ulrich Theodosius Aepinus<br>(1887) George Polya                                                                                         | RM131                                                                                                                          |                |
| 51 | 14 | M                                                                                                                                                     | (1546) Tycho Brahe                                                                                                             |                |
| 15 | T  | (1802) János Bolyai<br>(1923) Freeman John Dyson                                                                                                      | RM083                                                                                                                          |                |
| 16 | W  | (1804) Wiktor Yakovievich Bunyakowsky                                                                                                                 |                                                                                                                                |                |
| 17 | T  | (1706) Gabrielle Emile Le Tonnelier de Breteuil du Chatelet<br>(1835) Felice Casorati<br>(1842) Marius Sophus Lie<br>(1900) Dame Mary Lucy Cartwright |                                                                                                                                |                |
| 18 | F  | (1856) Joseph John Thomson<br>(1917) Roger Lyndon<br>(1942) Lenore Blum                                                                               | RM161                                                                                                                          |                |
| 19 | S  | (1783) Charles Julien Brianchon<br>(1854) Marcel Louis Brillouin<br>(1887) Charles Galton Darwin                                                      | RM138                                                                                                                          |                |
| 20 | S  | (1494) Oronce Fine<br>(1648) Tommaso Ceva<br>(1875) Francesco Paolo Cantelli                                                                          |                                                                                                                                |                |
| 52 | 21 | M                                                                                                                                                     | (1878) Jan Łukasiewicz<br>(1921) Edith Hirsch Luchins<br>(1932) John Robert Ringrose                                           |                |
| 22 | T  | (1824) Francesco Brioschi<br>(1859) Otto Ludwig Hölder<br>(1877) Tommaso Boggio<br>(1887) Srinivasa Aiyangar Ramanujan                                | RM150                                                                                                                          |                |
| 23 | W  | (1872) Georgii Yurii Pfeiffer                                                                                                                         |                                                                                                                                |                |
| 24 | T  | (1822) Charles Hermite<br>(1868) Emmanuel Lasker                                                                                                      | RM095<br>RM167                                                                                                                 |                |
| 25 | F  | (1642) Isaac Newton<br>(1900) Antoni Zygmund                                                                                                          | RM071                                                                                                                          |                |
| 26 | S  | (1780) Mary Fairfax Greig Somerville<br>(1791) Charles Babbage<br>(1937) John Horton Conway                                                           | RM059<br>RM119                                                                                                                 |                |
| 27 | S  | (1571) Johannes Kepler<br>(1654) Jacob (Jacques) Bernoulli                                                                                            | RM093                                                                                                                          |                |
| 53 | 28 | M                                                                                                                                                     | (1808) Athanase Louis Victoire Duprè<br>(1882) Arthur Stanley Eddington<br>(1903) John von Neumann                             | RM179<br>RM107 |
| 29 | T  | (1856) Thomas Jan Stieltjes                                                                                                                           |                                                                                                                                |                |
| 30 | W  | (1897) Stanislaw Saks                                                                                                                                 |                                                                                                                                |                |
| 31 | T  | (1872) Volodymyr Levitsky<br>(1896) Carl Ludwig Siegel<br>(1945) Leonard Adleman<br>(1952) Vaughan Frederick Randall Jones                            | RM143                                                                                                                          |                |



**Putnam 2000, B6**

Let  $B$  a set of more than  $\frac{2^{n+1}}{n}$  distinct point with coordinates of the form  $(\pm 1, \pm 1, \dots, \pm 1)$  in  $n$ -dimensional space with  $n \geq 3$ . Show that there are three distinct points in  $B$  which are the vertices of an equilateral triangle.

**English Jokes that only intellectuals understand**

Jean-Paul Sartre is sitting at a French café, revising his draft of Being and Nothingness. He says to the waitress: "I'd like a cup of coffee, please. With no cream". The waitress replies: "I'm sorry, Monsieur, but we're out of cream. How about one with no milk?"

**Headlines from a Mathematical World**

*Local Heat Wave Seen as Sign of Global Warming.*

Mathematically Literate World: Local Heat Wave Not Seen as Meaningful Indicator of Global Trends.

*I am now convinced that theoretical physics is actual philosophy.*

Max Born

*Now it is quite clear to me that there are no solid spheres in the heavens, and those that have been devised by the authors to save the appearances, exist only in the imagination.*

Tycho Brahe

*Math seems to provide us with a kind of new sense.*

Charles Galton Darwin

*To a physicist, mathematics is not only a tool through which you can compute the phenomena; it is the main source of concepts and principles, by which you create new theories.*

Freeman John Dyson

*We used to think that if we knew one, we knew two, because one and one are two. We are finding that we must learn a great deal more about 'and'.*

Arthur Stanley Eddington

*We are servants rather than masters in mathematics.*

Charles Hermite

*Nothing has afforded me so convincing a proof of the unity of the Deity as these purely mental conceptions of numerical and mathematical science which have been by slow degrees vouchsafed to man, and are still granted in these latter times by the Differential Calculus, now superseded by the Higher Algebra, all of which must have existed in that sublimely omniscient Mind from eternity.*

Mary Fairfax Greig Somerville